

**GAUTENG DEPARTMENT OF EDUCATION
PREPARATORY EXAMINATION**

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**MATHEMATICS
(Second Paper)**

MEMORANDUM

NOTE:

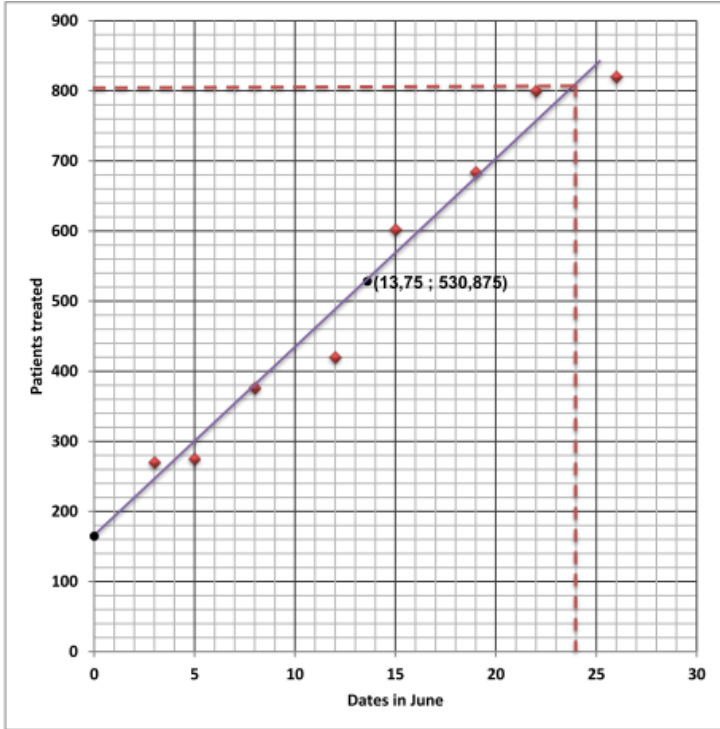
- If a candidate answered a question TWICE, mark the FIRST attempt ONLY.
- Consistent accuracy applies in ALL aspects of the memorandum.
- S/R refers to STATEMENT as well as REASON

QUESTION 1

1.1.	• Negatively skewed • <i>Negatief skeef</i>	✓negatively skewed / negatief skeef (1)
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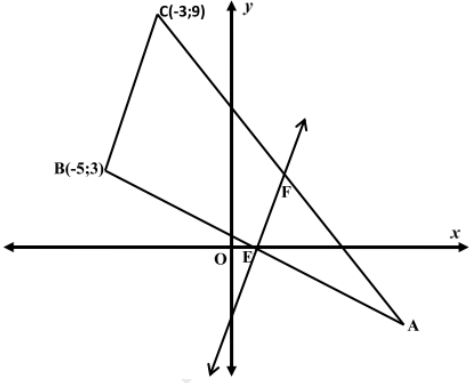
1.2 1.3	Cumulative Frequency Graph (Ogive) The graph is a cumulative frequency curve (ogive) plotted on a grid. The y-axis is labeled 'Cumulative Frequency' and ranges from 0 to 100 in increments of 10. The x-axis is labeled 'Risk interval' and ranges from 0 to 70 in increments of 10. The curve starts at the origin (0,0) and passes through the following points: (10, 2), (30, 6), (40, 14), (50, 28), (60, 60), and (70, 96). A horizontal dashed line is drawn at a cumulative frequency of 48, which intersects the curve. A vertical dashed line is then drawn from this intersection point down to the x-axis, and this point on the x-axis is labeled Q_2.	1.2 ✓shape ✓grounding at 10 ✓✓accuracy of points Subtract a mark if grounded at (0; 0) and/or at the end (4) 1.3 ✓ Q_2 shown on the graph, linked to cumulative frequency (1) [6]
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QUESTION 2

2.1		✓✓✓ points plotted correctly -1 for every 2 mistakes -1 if points are joined (3)
2.2	$y = 26,88x + 161,24$	✓ value of A = 161,24 ✓ value of B = 26,88 ✓ equation of the line (3)
2.3	$y = 26,88(24) + 161,24$ $y = 806,36$ 806 people treated on 24 th of June CANNOT USE GRAPH – NO LINE OF BEST FIT DRAWN YET	✓ substitute in formula ✓ answer as Natural Number (2)
2.4	See grid	✓ straight line ✓ graph passes through $(\bar{x} ; \bar{y})$ ✓ graph passes through y-intercept from regression line formula (3)
2.5	$r = 0,98$ This is a very strong positive, linear correlation. As the days increase the number of patients increase <i>Hierdie is 'n baie sterk positiewe lineêre korrelasie.</i> <i>Soos wat die dae vermeerder, vermeerder die getal pasiënte</i>	✓✓ correct answer ✓ interpretation (3)
2.6	This point is clearly an outlier/ <i>Die punt is 'n duidelike uitskieter</i> The 16 th of June is a public holiday and people might have decided to wait for the next day or certain medical facilities might have been closed. <i>Die 16de Junie is 'n publieke vakansiedag en mense het dalk besluit om te wag tot die volgende dag of sekere mediese fasiliteite kon dalk gesluit gewees het.</i>	✓ outlier/ uitskieter ✓ justification (2) [16]

QUESTION 3

3.1	$\begin{aligned} QR &= \sqrt{(x_Q - x_R)^2 + (y_Q - y_R)^2} \\ &= \sqrt{(1-7)^2 + (3-0)^2} \\ &= \sqrt{45} \\ &= 3\sqrt{5} \\ \therefore a &= 3 \end{aligned}$ OR $\begin{aligned} QR &= \sqrt{(x_Q - x_R)^2 + (y_Q - y_R)^2} \\ a\sqrt{5} &= \sqrt{(1-7)^2 + (3-0)^2} \\ a\sqrt{5} &= \sqrt{45} \\ 5a^2 &= 45 \\ a^2 &= 9 \\ a &= 3 ; a > 0 \end{aligned}$ OR $\begin{aligned} QR^2 &= (x_Q - x_R)^2 + (y_Q - y_R)^2 \\ 5a^2 &= (1-7)^2 + (3-0)^2 \\ 5a^2 &= 45 \\ a^2 &= 9 \\ a &= 3 ; a > 0 \end{aligned}$	✓ substitution in correct formula ✓ answer for QR ✓ $a = 3$ (3) ✓ substitution in correct formula ✓ $5a^2 = 45$ Squaring both side ✓ $a = 3 ; a > 0$ (3) ✓ substitution in correct formula ✓ $5a^2 = 45$ Squaring both side ✓ $a = 3 ; a > 0$ (3)
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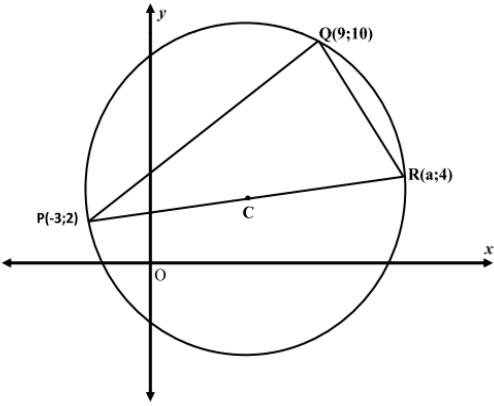
3.2	$3x + ty = -2$ $3(-3) + ty = -2$ $ty = 7 \dots\dots\dots(1)$ $y = -\frac{2}{3}x + 2$ $y = -\frac{2}{3}(-3) + 2$ $y = 4 \dots\dots\dots(2)$ $ty = 7$ $t(4) = 7$ $t = \frac{7}{4}$ OR $y = -\frac{2}{3}x + 2$ $3x + ty = -2$ $y = -\frac{3}{t}x - \frac{2}{t}$ $-\frac{3}{t}x - \frac{2}{t} = -\frac{2}{3}x + 2$ $-\frac{3(-3)}{t} - \frac{2}{t} = -\frac{2(-3)}{3} + 2$ $t = \frac{7}{4}$	$\checkmark 3(-3) + ty = -2$ $\checkmark ty = 7$ $\checkmark y = 4$ $\checkmark \text{value of } t$ (4) $\checkmark y = -\frac{3}{t}x - \frac{2}{t}$ $\checkmark \text{equations equal}$ $\checkmark \text{substitute } x = -3$ $\checkmark \text{value of } t$ (4)
3.3.1	 $\tan \theta = m_{EB}$ $\tan \theta = \frac{3-0}{-5-1}$ $\tan \theta = -\frac{1}{2}$ OR $\theta = -26,565 \dots + 180^\circ$ $\theta = 153,43^\circ$	$\checkmark \text{gradient of EB} = -\frac{1}{2}$ $\checkmark \tan \theta = -\frac{1}{2}$ $\checkmark \theta = 153,43^\circ$ (3)

3.3.2	Equation of EF: $y - y_1 = m(x - x_1)$ $y - 0 = 3(x - 1)$ $y = 3x - 3$ $m_{BC} = m_{EF} = 3$	$\checkmark m_{BC} = \frac{9-3}{-3+5} = 3$ $\checkmark m_{BC} = m_{EF} = 3$ $\checkmark \text{substitute point } (1; 0)$ $\checkmark \text{equation of line}$
3.3.3	$\tan \hat{F}EA = 3$ (From line in 1.3.2) $\hat{F}EA = 71,57^\circ$ $\hat{B}EF = 153,43^\circ - 71,57^\circ$ $\angle$'s on a straight line/ $\angle$'e op rt lyn $\hat{B}EF = 81,86^\circ$ $\hat{E}BC = 180^\circ - 81,86^\circ$ $\hat{E}BC = 98,14^\circ$ (co-interior angles /ko-binnehoeke; $EF \parallel BC$)	$\checkmark \hat{F}EA = 71,57^\circ$ $\checkmark \hat{B}EF = 81,86^\circ$ $\checkmark \hat{E}BC = 98,14^\circ$

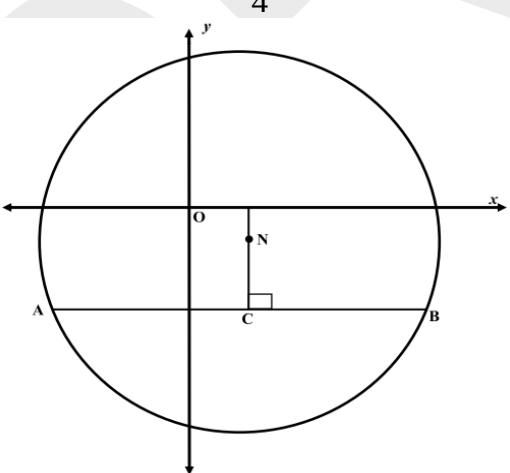
(4)

(3)
[17]

QUESTION 4

4.1.1	 $\hat{Q} = 90^\circ$ ($\angle$ in semi-circle/ $\angle$ in halfsirkel) $m_{PQ} \cdot m_{QR} = -1$ $\frac{10-4}{9-a} \times \frac{10-2}{9+3} = -1$ $\frac{6}{9-a} \times \frac{8}{12} = -1$ $\frac{4}{9-a} = -1$ $4 = -9 + a$ $a = 13$	$\checkmark \hat{Q} = 90^\circ$ $\checkmark \text{subs into } m_{PQ} \cdot m_{QR} = -1$ $\checkmark \text{simplification}$
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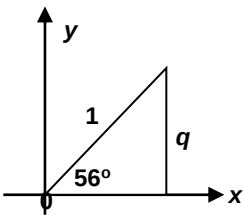
(3)

4.1.2	midpoint of PR $C\left(\frac{-3+13}{2}; \frac{4+2}{2}\right)$ $C(5; 3)$ $r = \sqrt{(13-5)^2 + (4-3)^2} \quad \text{or} \quad r^2 = (13-5)^2 + (4-3)^2$ $= \sqrt{65} \quad r^2 = 65$ Eq of circle: $(x-a)^2 + (y-b)^2 = r^2$ $(x-5)^2 + (y-3)^2 = 65$	✓ C (5; 3) ✓ substitute in distance formula ✓ $r = \sqrt{65} / r^2 = 65$ ✓ $(x-5)^2 + (y-3)^2 = 65$ (4)
4.2	$r_A = 3$ and A(2 ; 3) $r_B = 4$ and B(1 ; -1) $\therefore r_A + r_B = 7$ Distance between A and B $AB = \sqrt{(x_B - x_A)^2 + (y_B - y_A)^2}$ $AB = \sqrt{(1-2)^2 + (-1-3)^2}$ $= \sqrt{1+16}$ $= \sqrt{17}$ $\therefore r_A + r_B > \sqrt{17}$ The circles intersect each other	✓ radius and centre of circle A ✓ radius and centre of circle B ✓ sum of two radii ✓ calculating distance between centres ✓ $AB = \sqrt{17}$ ✓ correct conclusion (6)
4.3	$x^2 - 4x + y^2 + 2y = \frac{149}{4}$ 	
4.3.1	$(x-2)^2 - 4 + (y+1)^2 - 1 = \frac{149}{4}$ $(x-2)^2 + (y+1)^2 = \frac{169}{4}$ N(2;-1)	✓ completing the square ✓ standard form ✓ N(2;-1) (3)

4.3.2	$r^2 = \frac{169}{4}$ $r = \frac{13}{2} \quad \text{OR} \quad r = 6\frac{1}{2} \quad \text{OR} \quad r = 6,5$	✓ answer of radius (1)
4.3.3	NC ⊥ AB ∴ AC = CB = 6 (line from centre ⊥ chord/ lyn van midpt van sirkel ⊥ op koord) $x_A = 2 - 6 = -4$ Substitute $x = -4$ in $(-4)^2 - 4(-4) + y^2 + 2y = \frac{149}{4}$ $32 + y^2 + 2y = \frac{149}{4}$ $128 + 4y^2 + 8y = 149$ $4y^2 + 8y - 21 = 0$ $(2y - 3)(2y + 7) = 0$ $y = \frac{3}{2} \quad \text{or} \quad y = -\frac{7}{2}$ invalid $y < 0$ $A\left(-4; -\frac{7}{2}\right)$ and $B\left(8; -\frac{7}{2}\right)$	✓ AC = CB = 6 ✓ $x_A = -4$ ✓ substitute $x = -4$ ✓ coordinates of A ✓ coordinates of B (5) [22]

QUESTION 5

5.1.1	$\frac{b}{a} = \tan 110^\circ$	✓ $\tan 110^\circ$ (1)
5.1.2	$\frac{b}{\sqrt{a^2 + b^2}} = \sin 110^\circ$ $= 0,94$	✓ $\sin 110^\circ$ ✓ answer (2)
5.2.1	$\cos 146^\circ = \cos (90^\circ + 56^\circ)$ $= -\sin 56^\circ$ $= -q$ OR $\cos(180^\circ - 34^\circ)$ $= -\cos 34^\circ$ $= -\sin 56^\circ$ $= -q$	✓ $-\sin 56^\circ$ ✓ answer (2) ✓ $-\sin 56^\circ$ ✓ answer (2)

5.2.2	 $x^2 = r^2 - y^2$ $= 1^2 - q^2$ $\therefore x = \sqrt{1 - q^2}$ $\sin 112^\circ$ $= 2 \sin 56^\circ \cos 56^\circ$ $= 2q\sqrt{1 - q^2}$ OR $\cos^2 56^\circ + \sin^2 56^\circ = 1$ $\cos 56^\circ = \sqrt{1 - \sin^2 56^\circ}$ $= \sqrt{1 - q^2}$ $\sin 112^\circ$ $= 2 \sin 56^\circ \cos 56^\circ$ $= 2q\sqrt{1 - q^2}$	$\checkmark x = \sqrt{1 - q^2}$ $\checkmark 2 \sin 56^\circ \cos 56^\circ$ $\checkmark \text{answer}$ (3) $\checkmark \cos 56^\circ = \sqrt{1 - q^2}$ $\checkmark 2 \sin 56^\circ \cos 56^\circ$ $\checkmark \text{answer}$ (3) [8]
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QUESTION 6

6.1	$\cos(P + Q) = \cos P \cos Q - \sin P \sin Q$	$\checkmark$ correct formula (1)
6.2	$\cos 2P = \cos P \cos P - \sin P \sin P$ $= \cos^2 P - \sin^2 P$ $= \cos^2 P - (1 - \cos^2 P)$ $= 2 \cos^2 P - 1$	$\checkmark \cos P \cos P - \sin P \sin P$ $\checkmark$ replacing $\sin^2 P$ with $1 - \cos^2 P$ $\checkmark 2 \cos^2 P - 1$ (3)
6.3.1	$LHS = \frac{\sin 2x - \cos 2x + 1}{\sin 2x + \cos 2x + 1}$ $= \frac{2 \sin x \cos x - (1 - 2 \sin^2 x) + 1}{2 \sin x \cos x + (2 \cos^2 x - 1) + 1}$ $= \frac{2 \sin^2 x + 2 \sin x \cos x}{2 \cos^2 x + 2 \sin x \cos x}$ $= \frac{2 \sin x (\sin x + \cos x)}{2 \cos x (\cos x + \sin x)}$ $= \frac{\sin x}{\cos x}$ $= \tan x$ $= RHS$	$\checkmark 2 \sin x \cos x$ $\checkmark 1 - 2 \sin^2 x$ $\checkmark 2 \cos^2 x - 1$ $\checkmark$ factors $\checkmark \frac{\sin x}{\cos x}$ (5)

	OR $ \begin{aligned} LHS &= \frac{\sin 2x - \cos 2x + 1}{\sin 2x + \cos 2x + 1} \\ &= \frac{2 \sin x \cos x - (\cos^2 x - \sin^2 x) + 1}{2 \sin x \cos x + (\cos^2 x - \sin^2 x) + 1} \\ &= \frac{2 \sin x \cos x - \cos^2 x + \sin^2 x + 1}{2 \sin x \cos x + \cos^2 x - \sin^2 x + 1} \\ &= \frac{2 \sin x \cos x + 2 \sin^2 x}{2 \sin x \cos x + 2 \cos^2 x} \\ &= \frac{2 \sin x (\cos x + \sin x)}{2 \cos x (\sin x + \cos x)} \\ &= \frac{\sin x}{\cos x} \\ &= \tan x \\ &= RHS \end{aligned} $	✓ $2 \sin x \cos x$ ✓ $\cos^2 x - \sin^2 x$ ✓ simplification ✓ factors ✓ $\frac{\sin x}{\cos x}$ (5)
6.3.2	$ \begin{aligned} \tan 22,5^\circ &= \frac{\sin 45^\circ - \cos 45^\circ + 1}{\sin 45^\circ + \cos 45^\circ + 1} \\ &= \frac{\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2} + 1}{\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} + 1} \\ &= \frac{1}{\frac{2\sqrt{2}}{2} + 1} \\ &= \frac{1}{\sqrt{2} + 1} \\ &= \frac{1}{\sqrt{2} + 1} \times \frac{\sqrt{2} - 1}{\sqrt{2} - 1} \\ &= \sqrt{2} - 1 \end{aligned} $ OR	✓ $\tan 22,5^\circ = \frac{\sin 45^\circ - \cos 45^\circ + 1}{\sin 45^\circ + \cos 45^\circ + 1}$ ✓ substitution of $\frac{\sqrt{2}}{2}$ ✓ answer (3)

	$\tan 22,5^\circ = \frac{\sin 45^\circ - \cos 45^\circ + 1}{\sin 45^\circ + \cos 45^\circ + 1}$ $= \frac{\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} + 1}{\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} + 1}$ $= \frac{1}{\frac{1+1}{\sqrt{2}} + 1}$ $= \frac{1}{\frac{2}{\sqrt{2}} + 1}$ $= \frac{1}{\frac{2}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} + 1}$ $= \frac{1}{\sqrt{2} + 1}$ $= \frac{1}{\sqrt{2} + 1} \times \frac{\sqrt{2} - 1}{\sqrt{2} - 1}$ $= \sqrt{2} - 1$	✓ $\tan 22,5^\circ = \frac{\sin 45^\circ - \cos 45^\circ + 1}{\sin 45^\circ + \cos 45^\circ + 1}$ ✓ substitution of $\frac{1}{\sqrt{2}}$ ✓ answer (3)
6.4.1	$\sin 2x \cdot \cos 2x$ $= \frac{1}{2} \cdot 2 \sin 2x \cdot \cos 2x$ $= \frac{1}{2} \sin 4x$ $= \frac{1}{2} \cdot 1$ $= \frac{1}{2}$	✓ $\frac{1}{2} \cdot 2 \sin 2x \cdot \cos 2x$ ✓ max of $\sin 4x = 1$ ✓ $\frac{1}{2}$ (3)
6.4.2	$\sin 4x = 1$ $4x = 90^\circ + k \cdot 360^\circ \quad k \in \mathbb{Z}$ $x = 22,5^\circ + k \cdot 90^\circ \quad k \in \mathbb{Z}$ $x = -67,5^\circ$	✓ $\sin 4x = 1$ ✓ $4x = 90^\circ + k \cdot 360^\circ \quad k \in \mathbb{Z}$ ✓ $x = 22,5^\circ + k \cdot 90^\circ$ ✓ $x = -67,5^\circ$ (4)

[19]

QUESTION 7

7.1		f: ✓ shape ✓✓ intercepts ✓✓ turning points g: ✓ shape ✓✓ intercepts ✓✓ turning points	(6)
7.2	180°	✓ answer	(1)
7.3	$h(x) = -\frac{1}{2} \sin(x - 90^\circ)$ OR $h(x) = -\frac{1}{2} \sin[-(90^\circ - x)]$ $= -\frac{1}{2} [-\sin(90^\circ - x)]$ $\therefore h(x) = \frac{1}{2} \cos x$	✓✓ correct equation $\checkmark -\frac{1}{2} \sin[-(90^\circ - x)]$ $\checkmark \frac{1}{2} \cos x$	(2) (2)
7.4	$\cos 2x = 1$ $2x = 0^\circ + k \cdot 360^\circ, k \in \mathbb{Z}$ $x = 0^\circ + k \cdot 180^\circ, k \in \mathbb{Z}$ OR $\cos 2x = 1$ $2x = k \cdot 360^\circ, k \in \mathbb{Z}$ $x = k \cdot 180^\circ, k \in \mathbb{Z}$	$\checkmark 2x = 0^\circ + k \cdot 360^\circ, k \in \mathbb{Z}$ $\checkmark x = 0^\circ + k \cdot 180^\circ$ $\checkmark 2x = k \cdot 360^\circ, k \in \mathbb{Z}$ $\checkmark x = k \cdot 180^\circ$	(2) (2) [11]

QUESTION 8

8.1	In $\triangle MPQ$: $\frac{PM}{\sin z} = \frac{d}{\sin(180^\circ - (y + z))}$ $\therefore PM = \frac{d \sin z}{\sin(y + z)} \quad \dots\dots 1$ In $\triangle MPN$: $\frac{MN}{PM} = \sin x$ $MN = PM \sin x \quad \dots\dots 2$ $\therefore MN = \frac{d \sin z \cdot \sin x}{\sin(y + z)}$	$\checkmark \text{ correct substitution into sine rule}$ $\checkmark PM = \frac{d \sin z}{\sin(y + z)}$ $\checkmark \frac{MN}{PM} = \sin x$ $\checkmark \text{ substituting for PM into equation 2 and final answer}$	(4)
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8.2	$MN = \frac{1000 \sin y \sin(90^\circ - y)}{\sin 2y}$ $= \frac{1000 \sin y \cos y}{2 \sin y \cos y}$ $= 500 \text{ m}$	✓ correct replacement of angles ✓ $2 \sin y \cos y$ ✓ Answer (3) [7]
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QUESTION 9

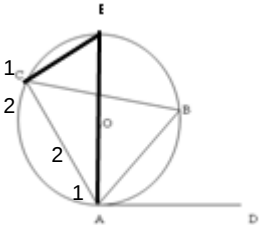
9.1	...perpendicular / ...loodreg	✓ perpendicular /loodreg (1)
9.2.1	$AB \perp CD$ (line from centre to midpoint of chord) / (lyn van die midpt van sirkel na midpt van koord) $DB = 9 \text{ cm}$ (AD = DB/ Given) In $\triangle DCB$ $(CD)^2 = (24)^2 - (9)^2$ (pythagoras) $CD^2 = 576 - 81$ $= 495$ $CD = 3\sqrt{55}$	✓ S/R [S/R Statement and reason] ✓ DB = 9 cm ✓ using Theorem of Pythagoras(S/R) ✓ $CD = 3\sqrt{55}$ (4)
9.2.2	$\frac{CD}{DE} = 3$ $\frac{3\sqrt{55}}{DE} = 3$ $DE = \sqrt{55}$	✓ $\frac{3\sqrt{55}}{DE} = 3$ ✓ $DE = \sqrt{55}$ (2) [7]

QUESTION 10

10.1	$\hat{E}_1 = 90^\circ$ ($\angle$ in a semi-circle / $\angle$ in halwe sirkel)	✓ $\hat{E}_1 = 90^\circ$ ✓ $\angle$ in a semi-circle (2)
10.2	$\hat{E}_1 = 90^\circ$ ($\angle$ in a semi-circle / $\angle$ in halwe sirkel) $\hat{E} + \hat{A}_2 = 180^\circ$ (opp $\angle$'s cyclic quad / oorst $\angle$ 'e van kvh) $\therefore \hat{A}_2 = 180^\circ - (90^\circ + 28^\circ)$ $= 62^\circ$ OR	✓ $\hat{E} + \hat{A}_2 = 180^\circ$ ✓ opp $\angle$'s cyclic quad ✓ $\hat{A}_2 = 62^\circ$ (3)

	$\hat{FAC} = 90^\circ$ ($\angle$ in a semi-circle / $\angle$ in halwe sirkel) $\hat{A}_3 = 28^\circ$ ($\angle$'s in the same segment subt by DC / $\angle$ in dieselfde segment onderspdeur DC) $\therefore \hat{A}_2 = 90^\circ - 28^\circ$ $= 62^\circ$	$\checkmark \hat{FAC} = 90^\circ$ S/R $\checkmark \hat{A}_3 = 28^\circ$ S/R $\checkmark \hat{A}_2 = 62^\circ$
10.3	$\hat{F}_2 = 30^\circ$ (equal chords subtend equal $\angle$'s) / (gelyke koorde onderspan gelyke hoek)	$\checkmark \hat{F}_2 = 30^\circ$ $\checkmark$ equal chord subtend eq $\angle$'s
		(3) (2) [7]

QUESTION 11

11.1	 Construction: Draw a diameter/ <i>middel</i>lyn AOE and join CE Proof: $\hat{A}_1 + \hat{A}_2 = 90^\circ$ (tan/rk lyn $\perp$ radius) $\hat{C}_1 + \hat{C}_2 = 90^\circ$ ($\angle$ in a semi circle / $\angle$ in halwe sirkel) but $\hat{C}_1 = \hat{A}_2$ ($\angle$'s in the same segment) $\therefore \hat{A}_1 = \hat{C}_2$	$\checkmark$ construction $\checkmark \hat{A}_1 + \hat{A}_2 = 90^\circ$ $\checkmark$ tang $\perp$ radius $\checkmark \hat{C}_1 + \hat{C}_2 = 90^\circ$ (S/R) $\checkmark \hat{C}_1 = \hat{A}_2$ (S/R)
11.2.1	$\hat{C}_1 = 90^\circ$ ($\angle$ in a semi circle / $\angle$ in halwe sirkel) $\hat{D}_1 = 90^\circ$ (OE $\perp$ BC) $\hat{C}_1 = \hat{D}_1$ $\therefore OE \parallel AC$ (corr $\angle$'s are equal / ooreenk $\angle$ is gelyk) OR $\hat{C}_1 = 90^\circ$ ($\angle$ in a semi circle / $\angle$ in halwe sirkel) $\hat{D}_2 = 90^\circ$ (OE $\perp$ BC) $\hat{C}_1 + \hat{D}_2 = 180^\circ$ $\therefore OE \parallel AC$ (co interior $\angle$'s are equal / ko – binne $\angle$ is gelyk)	$\checkmark \hat{C}_1 = 90^\circ$ (S/R) $\checkmark \hat{D}_1 = 90^\circ$ (S/R) $\checkmark \hat{C}_1 = \hat{D}_1$ (S) $\checkmark$ corr $\angle$'s are equal $\checkmark \hat{C}_1 = 90^\circ$ (S/R) $\checkmark \hat{D}_{21} = 90^\circ$ (S/R) $\checkmark \hat{C}_1 + \hat{D}_2 = 180^\circ$ (S) $\checkmark$ co interior $\angle$'s are equal
		(5) (4) (4)

11.2.2	$\hat{A} = x$ (tan chord / rk lyn koord) $\hat{O}_1 = x$ (corr $\angle^s$ / ooreenk $\angle^e$ OE $\parallel$ AC)	$\checkmark \hat{A} = x$ $\checkmark$ tan chord $\checkmark \hat{O}_1 = x$ S/R (3)
11.2.3	In $\triangle PAC$ $\hat{P} = 180^\circ - x - 90^\circ - x$ (sum of $\angle^s$ of a triangle/ $= 90^\circ - 2x$ som van $\angle^e$ van driehoek)	$\checkmark \hat{P} = 90^\circ - 2x$ $\checkmark$ sum of $\angle^s$ of a triangle (2) [14]

QUESTION 12

12.1	proportionally	$\checkmark$ proportionally (1)
12.2.1	$\hat{C}_1 = \hat{C}_2$ (given) $\hat{C}_1 = \hat{D}$ (corr $\angle^s$ / ooreenk $\angle^e$ AD $\parallel$ CG) $\hat{C}_2 = \hat{A}_1$ (alt $\angle^s$ / verwisselende $\angle^e$ AD $\parallel$ CG) $\therefore \hat{A}_1 = \hat{D}$ $\therefore CA = CD$ (sides opp equal $\angle^s$ / sy teenoor gelyke $\angle^e$)	$\checkmark \hat{C}_1 = \hat{D}$ (S/R) $\checkmark \hat{C}_2 = \hat{A}_1$ (S/R) $\checkmark \hat{A}_1 = \hat{D}$ $\checkmark CA = CD$ (S/R) (4)
12.2.2	$\frac{BC}{CD} = \frac{BG}{GA}$ (line $\parallel$ to one side of $\triangle$ / lyn $\parallel$ een sy van $\triangle$) but $CA = CD$ (proved) $\therefore \frac{BC}{AC} = \frac{BG}{AG}$	$\checkmark \frac{BC}{CD} = \frac{BG}{GA}$ $\checkmark$ $\checkmark$ replace $CD = CA$ (3)
12.3.1	In $\triangle KMT$ and $\triangle KON$ $\hat{M}_1 = \hat{O}$ (ext. $\angle$ of a cyclic quad / buite $\angle$ kvh) $\hat{T}_2 = \hat{N}$ (ext. $\angle$ of a cyclic quad / buite $\angle$ kvh) $\hat{K} = \hat{K}$ (common / gemeensk) $\therefore \triangle MTK \parallel \triangle ONK$ ($\angle \angle \angle$)	$\checkmark \checkmark$ for any two of the three statements $\checkmark$ equiangular / gelykhoekig / $\angle \angle \angle$ (3)
12.3.2	$\frac{MT}{ON} = \frac{TK}{NK} = \frac{MK}{OK}$ $\therefore KM \cdot KN = KT \cdot KO$	$\checkmark \frac{MT}{ON} = \frac{TK}{NK} = \frac{MK}{OK}$ (1)

12.3.2	$\frac{MK}{OK} = \frac{KT}{NK}$ $\frac{5}{6+KT} = \frac{KT}{8}$ $KT^2 + 6KT = 40$ $KT^2 + 6KT - 40 = 0$ $(KT+10)(KT-4) = 0$ $KT = -10 \text{ or } KT = 4$ $\therefore KT = 4 \text{ units}$	$\checkmark \frac{5}{6+KT} = \frac{KT}{8}$ $\checkmark KT^2 + 6KT - 40 = 0$ $\checkmark \text{factors}$ $\checkmark \text{answer}$ (4) [16]
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TOTAL: 150