

FINAL



KWAZULU-NATAL PROVINCE

EDUCATION
REPUBLIC OF SOUTH AFRICA

MATHEMATICS P1

COMMON TEST

SEPTEMBER 2024

MARKING GUIDELINES

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MARKS: 150

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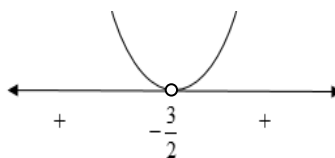
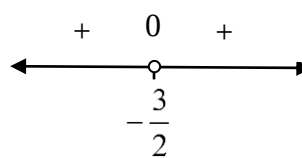
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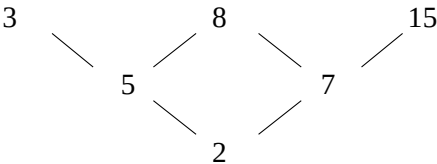
QUESTION 1

1.1.1	$x(x-5) = 0$ $x = 0$ or $x = 5$ Answer only: Full marks	✓ A factors ✓ A answer (0) ✓ CA answer (5) (3)
1.1.2	$x = \frac{-2 \pm \sqrt{(2)^2 - 4(5)(-6)}}{2(5)}$ $x = 0,91$ or $-1,31$ Answer only: 2/3 Penalise for incorrect rounding only in this question.	✓ A substitution into formula ✓ CA answer ✓ CA answer (3)
1.1.3	$2^x(2 - 3 \cdot 2^{-1} + 1) = 12$ $2^x \left(3 - \frac{3}{2} \right) = 12$ $2^x \left(\frac{3}{2} \right) = 12$ $2^x = 8$ $2^x = 2^3$ OR $x = \log_2 8$ $\therefore x = 3$	✓ A factors ✓ CA prime bases (or use of logarithms) ✓ CA answer (3)
1.1.4	$(2x+3)(2x+3) > 0$ CV: $-\frac{3}{2}$  OR  $x \in \mathbb{R}$, but $x \neq -\frac{3}{2}$ OR $x < -\frac{3}{2}$ or $x > -\frac{3}{2}$ OR $\left(-\infty; -\frac{3}{2} \right)$ or $\left(-\frac{3}{2}; \infty \right)$	✓ A factors ✓ A $x \in \mathbb{R}$; ✓ CA $x \neq -\frac{3}{2}$ (3)

GRADE 12
Marking Guideline

1.2	$2x - y + 1 = 0$ $y = 2x + 1$ $x^2 + x(2x + 1) - (2x + 1) = 3x - 2$ $x^2 + 2x^2 + x - 2x - 1 - 3x + 2 = 0$ $3x^2 - 4x + 1 = 0$ $(3x - 1)(x - 1) = 0$ $x = \frac{1}{3} \text{ or } 1$ $y = 2\left(\frac{1}{3}\right) + 1 = \frac{5}{3}$ $y = 2(1) + 1 = 3$ OR $2x - y + 1 = 0$ $2x = y - 1$ $x = \frac{y - 1}{2}$ $\left(\frac{y - 1}{2}\right)^2 + y\left(\frac{y - 1}{2}\right) - y = 3\left(\frac{y - 1}{2}\right) - 2$ $\frac{y^2 - 2y + 1}{2} + \frac{y^2 - y}{2} - y = \frac{3y - 3}{2} - 2$ $y^2 - 2y + 1 + 2y^2 - 2y - 4y = 6y - 6 - 8$ $3y^2 - 8y + 1 = 6y - 14$ $3y^2 - 14y + 15 = 0$ $(3y - 5)(y - 3) = 0$ $y = \frac{5}{3} \text{ or } 3$ $x = \frac{\frac{5}{3} - 1}{2} = \frac{1}{3}$ $x = \frac{3 - 1}{2} = 1$	✓A $y = 2x + 1$ ✓CA substitution ✓CA standard form ✓CA x-values ✓CA y-values (5) OR ✓A $x = \frac{y - 1}{2}$ ✓CA substitution ✓CA standard form ✓CA y-values ✓CA x-values (5)
1.3	$x^2 - 2x - 3 = y^2 - 2y - 3$ $x^2 - y^2 - 2x + 2y = 0$ $(x + y)(x - y) - 2(x - y) = 0$ $(x - y)(x + y - 2) = 0$ $x - y = 0 \quad x + y - 2 = 0$ $\text{N/A} \quad x = 2 - y$	✓A expanding ✓CA standard form ✓A factors $(x + y)(x - y)$ ✓CA factors ✓CA answer $x = 2 - y$ only (5)
		[22]

QUESTION 2

2.1.1	 $2a = 2$ $a = 1$ $5 = 3(1) + b$ $b = 2$ $3 = 1 + 2 + c$ $c = 0$ $T_n = n^2 + 2n$	✓ A $a = 1$ ✓ CA $b = 2$ ✓ CA $c = 0$ ✓ CA answer (4)
2.1.2	$n^2 + 2n = 1700$ $n^2 + 2n - 1700 = 0$ $n = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $n = \frac{-2 \pm \sqrt{2^2 - 4(1)(1700)}}{2(1)}$ $n = 40, 24 \text{ or } n = -42, 24$ n is not a natural number and therefore 1700 is not a term in the sequence.	✓ CA equating T_n to 1700 ✓ CA substitution into formula ✓ CA values of n ✓ CA 1700 is not a term in the sequence (4)

2.2	$(1-2)(1+2) + (3-4)(3+4) + (5-6)(5+6) + (7-8)(7+8) + \dots$ $\dots + (399-400)(399+400)$ $= (-1)(3) + (-1)(7) + (-1)(11) + (-1)(15) + \dots + (-1)(799)$ $= -3 - 7 - 11 - 15 - \dots - 799$ $a = -3 \quad d = 4$ $T_n = a + (n-1)d$ $-799 = -3 + (n-1)4$ $n = 200$ $S_n = \frac{n}{2}[2a + (n-1)d] \qquad \text{OR} \qquad S_n = \frac{n}{2}(a+l)$ $S_{200} = \frac{200}{2}[2(-3) + (200-1)(-4)] \qquad S_{200} = \frac{200}{2}(-3-799)$ $= -80200 \qquad \qquad \qquad = -80200$ OR $1^2 + 3^2 + 5^2 + 7^2 + \dots + 399^2$ $= (2n-1)^2$ $-2^2 - 4^2 - 6^2 - 8^2 - \dots - 400^2$ $= -(2n)^2$ $= (2n-1)^2 - (2n)^2$ $= 4n^2 - 4n + 1 - 4n^2$ $= -4n + 1$ $2n = 400 \quad \text{OR} \quad 2n-1 = 399$ $n = 200$ $\sum_{n=1}^{200} (-4n-1) = -3-7-11-\dots$ $S_n = \frac{n}{2}[2a + (n-1)d]$ $S_{200} = \frac{200}{2}[2(-3) + (200-1)(-4)]$ $= -80200$	✓ A factors ✓ A arithmetic series ✓ CA $n = 200$ ✓ CA substitution in S_n formula ✓ CA answer (5) OR ✓ A $(2n-1)^2 - (2n)^2$ ✓ A $-4n+1$ ✓ CA $n = 200$ ✓ CA substitution in S_n formula ✓ CA answer (5)
		[13]

QUESTION 3

3.1.1	$81; m; \frac{m}{3}; \dots\dots\dots$ $\frac{m}{81} = \frac{\frac{m}{3}}{m}$ $\frac{m}{81} = \frac{1}{3}$ OR $m^2 = \frac{81m}{3}$ $3m = 81$ $m^2 = 27m$ $m = 27$ $m = 27$ Answer only: Full marks	$\checkmark A \quad \frac{m}{81} = \frac{\frac{m}{3}}{m}$ $\checkmark A$ answer (2)
3.1.2	$\sum_{t=1}^9 81 \left(\frac{1}{3} \right)^{t-1} = 81 + 27 + 9 + 3 + \dots$ $a = 81$ $r = \frac{1}{3}$ $S_n = \frac{a(r^n - 1)}{r - 1}$ $S_9 = \frac{81 \left(\left(\frac{1}{3} \right)^9 - 1 \right)}{\frac{1}{3} - 1}$ $= \frac{9841}{81} = 121,49$	$\checkmark A$ value of a $\checkmark A$ value of r $\checkmark CA$ substitute into formula $\checkmark CA$ answer (4)
3.2.1	$a = \frac{12}{5}; \quad d = \frac{3}{5}; \quad T_n = \frac{333}{5}$ $T_n = a + (n-1)d$ $\frac{333}{5} = \frac{12}{5} + (n-1)\left(\frac{3}{5}\right)$ $333 = 12 + 3n - 3$ $333n = 324$ $n = 108$	$\checkmark A \quad d = \frac{3}{5}$ $\checkmark A$ substitute $\frac{333}{5}$ into formula $\checkmark CA$ substitute d into formula $\checkmark CA$ answer (4)

3.2.2	$\frac{12}{5}; 3; \frac{18}{5}; \frac{21}{5}; \frac{24}{5}; \frac{27}{5}; 6; \dots\dots\dots 66; \frac{333}{5}$ Terms that are integers: $3; 6; 9; \dots\dots\dots; 66$ $T_n = a + (n-1)d$ $66 = 3 + (n-1)3$ $66 = 3 + 3n - 3$ $3n = 66$ $n = 22$ OR The following terms are integers: $T_2; T_7; \dots\dots\dots T_{107}$ Sequence: $2; 7; 12; \dots\dots 107$ $T_n = a + (n-1)d$ $107 = 2 + (n-1)5$ $107 = 2 + 5n - 5$ $5n = 110$ $n = 22$	✓A identifying one more term that is an integer ✓A correct sequence ✓CA substitution ✓CA answer OR ✓A identifying the position of one more term that is an integer ✓A correct sequence ✓CA substitution ✓CA answer (4)
		[14]

QUESTION 4

4.1	$x^2 - 2x - 3 = 0$ $(x+1)(x-3) = 0$ $x = -1 \text{ or } x = 3$ $\therefore P(-1; 0) \quad Q(3; 0)$	✓ A factors ✓ CA answer ✓ CA answer (3)
4.2	At turning point: $x = \frac{-b}{2a}$ $= \frac{-(-2)}{2(1)}$ $= 1$ $y = 1^2 - 2(1) - 3 = -4$ $\therefore T(1; -4)$ OR $h(x) = (x^2 - 2x + 1) - 3 - 1$ $h(x) = (x-1)^2 - 4$ $\therefore T(1; -4)$ OR $x\text{-value at TP: } = \frac{x_1 + x_2}{2}$ $= \frac{-1 + 3}{2}$ $= 1$ $y = 1^2 - 2(1) - 3 = -4$ $\therefore T(1; -4)$ OR $h'(x) = 2x - 2 = 0$ $x = 1$ $y = 1^2 - 2(1) - 3 = -4$ $\therefore T(1; -4)$ Answer only: 2/3	✓ A substitution ✓ CA x-value ✓ CA y-value (3) OR ✓ A completing the square ✓ CA x-value ✓ CA y-value (3) OR ✓ CA average value of x-intercepts ✓ CA x-value ✓ CA y-value (3) OR ✓ A derivative = 0 ✓ CA x-value ✓ CA y-value (3)
4.3	$x = 0$	✓ A answer (1)
4.4	$g(x) = \frac{a}{x} - 2$ Substitute $P(-1; 0)$: $0 = \frac{a}{-1} - 2$ $a = -2$	✓ A $q = -2$ ✓ CA substitution ✓ CA answer (3)

4.5	Yes, it is a function For every x-value, there are only one y-value OR It passes the vertical line test.	✓A answer ✓A justification (2)
4.6	$x^2 - 2x - 3 = \frac{-2}{x} - 2$ $x^3 - 2x^2 - 3x = -2 - 2x$ $x^3 - 2x^2 - x + 2 = 0$ $x^2(x-2) - (x-2) = 0$ $(x-2)(x^2-1) = 0$ $(x-2)(x-1)(x+1) = 0$ $x = -1 \text{ or } x = 1 \text{ or } x = 2$ At K: $x = 2$ $y = \frac{-2}{2} - 2 = -3$ K(2 ; -3)	✓CA equating ✓CA simplification ✓CA factors ✓CA x value ✓CA y value (5)
4.7	$x \in (-1; 0) \text{ or } x \in (1; 2)$ OR $-1 < x < 0 \text{ or } 1 < x < 2$	✓CA ✓CA $x \in (-1; 0)$ ✓CA $x \in (1; 2)$ (3) OR ✓CA ✓CA $-1 < x < 0$ ✓CA $1 < x < 2$ (3) [20]

QUESTION 5

5.1	$-2x + 3 = 0$ $x = \frac{3}{2}$ Answer only: Full marks	✓A equating to 0 ✓A $x = \frac{3}{2}$ (2)
5.2	$-2^{-x+1} \cdot x + 6 \cdot 2^{-x-1} < 0$ $-2 \cdot 2^{-x} x + 6 \cdot 2^{-x} \cdot 2^{-1} < 0$ $-2x \cdot 2^{-x} + 3 \cdot 2^{-x} < 0$ $2^{-x}(-2x + 3) < 0$ $\frac{3}{2} < x \leq 3$	✓A splitting exponents ✓A factorisation ✓CA ✓CA answer (4)
5.3	$p: x = 2^{-y}$ $y = -\log_2 x$ OR $p: x = \left(\frac{1}{2}\right)^y$ $y = \log_{\frac{1}{2}} x$ Answer only: Full marks	✓A swapping x and y ✓CA answer (2) OR ✓A swapping x and y ✓CA answer (2)

5.4	range of f^{-1} = domain of f $-4 \leq y \leq 3$	✓✓ A A answer (2)
5.5	Intersection between $y = -2x + 3$ and $y = x$: $-2x + 3 = x$ $-3x = -3$ $x = 1$ $y = 1$ OR $f^{-1}: x = -2y + 3$ $y = \frac{-x + 3}{2}$ $-2x + 3 = \frac{-x + 3}{2}$ $x = 1$ $y = 1$ OR $x = \frac{-x + 3}{2}$ $x = 1$ $y = 1$	✓A $-2x + 3 = x$ ✓A x-value ✓A y-value (3) OR ✓A $-2x + 3 = \frac{-x + 3}{2}$ ✓A x-value ✓A y-value (3) OR ✓A $x = \frac{-x + 3}{2}$ ✓A x-value ✓A y-value (3)
		[12]

QUESTION 6

6.1	$A = P(1+i)^n$ $13460 = 6500\left(1+\frac{i}{4}\right)^{16}$ $\left(1+\frac{i}{4}\right)^{16} = \frac{13460}{6500}$ $1+\frac{i}{4} = \sqrt[16]{\frac{13460}{6500}}$ $i = 0,1862 = 18,6\%$ $r = 18,6$	✓ A $n = 16$ ✓ CA substitution ✓ CA $1+\frac{i}{4} = \sqrt[16]{\frac{13460}{6500}}$ ✓ CA answer (4)
6.2	$F = \frac{x[(1+i)^n - 1]}{i}; \quad n = 17$ $65000 = \frac{x\left[\left(1+\frac{0,08}{12}\right)^{17} - 1\right]}{\frac{0,08}{12}}$ $x = \frac{65000 \times \frac{0,08}{12}}{\left(1+\frac{0,08}{12}\right)^{17} - 1}$ $x = R3623,67$	✓ A $n = 17$ ✓ CA substitution ✓ CA answer (3)
6.3.1	$P = \frac{x[1-(1+i)^{-n}]}{i}$ $R650\,000 = \frac{7000\left[1-\left(1+\frac{0,11}{12}\right)^{-n}\right]}{\frac{0,11}{12}}$ $\frac{650\,000 \times \frac{0,11}{12}}{7000} = 1 - \left(1+\frac{0,11}{12}\right)^{-n}$ $\left(1+\frac{0,11}{12}\right)^{-n} = \frac{25}{168}$ $\log_{\left(1+\frac{0,11}{12}\right)}\left(\frac{25}{168}\right) = -n$ $n = 208,7788941$ 208 instalments of R7 000	✓ A substitution ✓ CA use of logarithms ✓ CA value of n ✓ CA answer (4)

GRADE 12

Marking Guideline

6.3.2	Outstanding balance at $T_{208} = \frac{7000 \left[1 - \left(1 + \frac{0,11}{12} \right)^{-0,7788941} \right]}{\frac{0,11}{12}}$ $= R5\ 408,18$ Final payment $= 5408,18 \left(1 + \frac{0,11}{12} \right)$ $= R5\ 457,75$ OR Outstanding balance at T_{208} $= 650000 \left(1 + \frac{0,11}{12} \right)^{208} - \frac{7000 \left[\left(1 + \frac{0,11}{12} \right)^{208} - 1 \right]}{\frac{0,11}{12}}$ $= R5\ 408,18$ Final payment $= 5408,18 \left(1 + \frac{0,11}{12} \right)$ $= R5\ 457,75$	✓CA value of n ✓CA substitution in present value formula ✓CA compounding ✓CA answer (4) OR ✓CA $= 650000 \left(1 + \frac{0,11}{12} \right)^{208}$ ✓CA $= \frac{7000 \left[\left(1 + \frac{0,11}{12} \right)^{208} - 1 \right]}{\frac{0,11}{12}}$ ✓CA compounding ✓CA answer (4)
		[15]

QUESTION 7

Penalise once only for incorrect notation in 7.1.

7.1	$f(x) = -x^2 + x$ $f(x+h) = -(x+h)^2 + (x+h) = -x^2 - 2xh - h^2 + x + h$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-x^2 - 2xh - h^2 + x + h - (-x^2 + x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-x^2 - 2xh - h^2 + x + h + x^2 - x}{h}$ $= \lim_{h \rightarrow 0} \frac{-2xh - h^2 + h}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-2x - h + 1)}{h}$ $= \lim_{h \rightarrow 0} (-2x - h + 1)$ $= -2x + 1$	✓ A value of $f(x+h)$ ✓ CA substitution into correct formula ✓ CA simplifying ✓ CA factors ✓ CA answer (5)
7.2.1	$y = x^3(4 - x^{-3})$ $y = 4x^3 - 1$ $\frac{dy}{dx} = 12x^2$	✓ A product ✓ CA answer (2)
7.2.2	$f(x) = \frac{2x^2 + 3}{\sqrt{x}}$ $f(x) = \frac{2x^2}{x^{\frac{1}{2}}} + \frac{3}{x^{\frac{1}{2}}}$ $f(x) = 2x^{\frac{3}{2}} - 3x^{-\frac{1}{2}}$ $f'(x) = 3x^{\frac{1}{2}} - \frac{3}{2}x^{-\frac{3}{2}}$	✓ A $2x^{\frac{3}{2}}$; ✓ A $-3x^{-\frac{1}{2}}$ ✓ CA $3x^{\frac{1}{2}}$; ✓ CA $-\frac{3}{2}x^{-\frac{3}{2}}$ (4)
		[11]

QUESTION 8

8.1	$0 = -\frac{1}{2}x + 2$ $\frac{1}{2}x = 2$ $x = 4$ $\therefore Q(4; 0)$	✓ A equating to zero ✓ A answer (2)
8.2	$n = -4$	✓ CA answer (1)
8.3	$0 = (x-1)^2(x-4)$ $x = 1 \text{ or } 4$ $PQ = 4 - 1 = 3 \text{ units}$	✓ CA values of x . ✓ CA answer (2)
8.4	$f(x) = x^3 - 6x^2 + 9x - 4$ $f'(x) = 3x^2 - 12x + 9$ $3x^2 - 12x + 9 = 0$ $x^2 - 4x + 3 = 0$ $(x-1)(x-3) = 0$ $x = 3$ $y = (3)^2 - 6(3) + 9(3) - 4 = -4$ $\therefore S(3; -4)$	✓ CA multiplying out ✓ CA derivative ✓ CA equating to zero ✓ CA value of x ✓ CA value of y (5)
8.5	f is concave down at $x = 0$.	✓ A concave down (1)
8.6	To determine where $f'(x) = \text{gradient of } h$: $\therefore 3x^2 - 12x + 9 = -\frac{1}{2}$ $3x^2 - 12x + \frac{19}{2} = 0$ $x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(3)\left(\frac{19}{2}\right)}}{2(3)}$ $x = 1,09 \text{ or } x = 2,91$	✓ CA equating derivative to $-\frac{1}{2}$ ✓ CA standard form ✓ CA substitution ✓ CA ✓ CA values of x (5)
		[16]

QUESTION 9

9.1	$h'(t) = 20 - 10t$ $0 = 20 - 10t$ $t = 2 \text{ seconds}$ Max height: $h(2) = -5(2)^2 + 20(2) + 1$ $= 21 \text{ metres}$	✓ A derivative ✓ CA equating derivative to zero ✓ CA value of t ✓ CA substitution ✓ CA answer (5)
9.2	$1 + 20t - 5t^2 = 0$ $5t^2 - 20t - 1 = 0$ $t = \frac{20 \pm \sqrt{(-20)^2 - 4(5)(-1)}}{2(5)}$ $t = -0,05 \text{ or } 4,05$ $t = 4,05 \text{ seconds}$	✓ A equating h to zero ✓ A values of t ✓ CA answer (3)
9.3	$h'(t) = 20 - 5t$ $h'(1,5) = 20 - 10(1,5)$ $= 5 \text{ m/s}$	✓ CA substitution in $h'(t)$ ✓ CA answer (2)
		[10]

QUESTION 10

10.1.1	$P(\text{Female}) = \frac{648}{864} = \frac{3}{4}$	✓ A answer (1)
10.1.2	$P(\text{Female}) \times P(\text{Positive}) = \frac{648}{864} \times \frac{108}{864}$ $= \frac{3}{32} = 0,09$ $P(\text{Female and Positive}) = \frac{81}{864}$ $= \frac{3}{32} = 0,09$ $P(\text{Female and Positive}) = P(\text{Female}) \times P(\text{Positive})$ Events are independent. Testing positive is independent of gender. OR $P(\text{Male}) \times P(\text{Positive}) = \frac{216}{864} \times \frac{108}{864}$ $= \frac{1}{32} = 0,03$ $P(\text{Male and Positive}) = \frac{27}{864}$ $= \frac{1}{32} = 0,03$ $P(\text{Male and Positive}) = P(\text{Male}) \times P(\text{Positive})$ Events are independent. Testing positive is independent of gender.	✓ A $P(\text{Female}) \times P(\text{Positive})$ ✓ A 0,09375 or 0,09 ✓ A $P(\text{Female and Positive}) = 0,09375$ or 0,09 ✓ A conclusion (4) OR ✓ A $P(\text{Male}) \times P(\text{Positive})$ ✓ A 0,03125 or 0,03 ✓ A $P(\text{Male and Positive}) = 0,03125$ or 0,03 ✓ A conclusion (4)
10.2.1	$20 \times 20 \times 10 \times 10 \times 20 \times 20$ = 16 000 000 number plates	✓ A $20 \times 20 \times 10 \times 10 \times 20 \times 20$ ✓ A answer (2)
10.2.2	$20 \times 19 \times 10 \times 9 \times 18 \times 17$ = 10 465 200 number plates Also accept: $18 \times 17 \times 10 \times 9 \times 16 \times 15$ = 6 609 600	✓ A $20 \times 19 \times 10 \times 9 \times 18 \times 17$ ✓ A answer (2)
10.2.3	$\frac{2 \times 1 \times 10 \times 9 \times 18 \times 17}{10\,465\,200}$ $= \frac{1}{190}$ Also accept: $\frac{2 \times 1 \times 10 \times 9 \times 16 \times 15}{6\,609\,600}$ $= \frac{1}{153}$	✓ A numerator ✓ A denominator ✓ CA answer (3)

GRADE 12

Marking Guideline

10.3	Let the number of red sweets be x. $P(\text{at least one green sweet}) = 1 - P(\text{no green sweets})$ $= 1 - \left(\frac{x}{10}\right)^4$ $1 - \left(\frac{x}{10}\right)^4 = 0,9744$ $\left(\frac{x}{10}\right)^4 = 1 - 0,9744$ $\left(\frac{x}{10}\right)^4 = 0,0256$ $\left(\frac{x}{10}\right) = \frac{2}{5}$ $x = 4$ There are 6 green sweets in the bag.	$\checkmark A \ 1 - \left(\frac{x}{10}\right)^4$ $\checkmark A \text{ equating to } 97,44\%$ $\checkmark CA \text{ value of } x$ $\checkmark CA \text{ answer}$ (4)
		[16]

TOTAL: 150